

El juego de la evolución



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Carlos III de Madrid

Sumario

- (1) Teoría de Juegos**
- (2) La evolución como un juego**
- (3) Ejemplos de la biología**
- (4) La evolución de la cooperación**

Teoría de Juegos

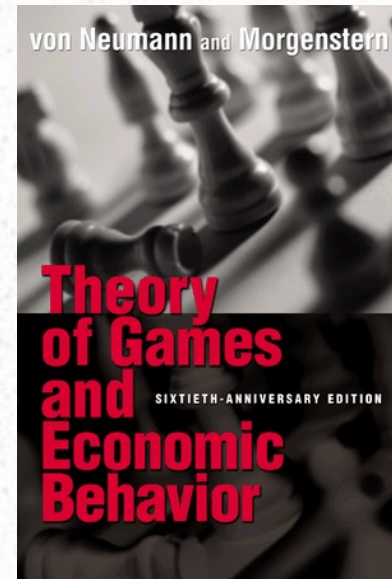
Origen



Von Neumann
(1903-1957)



Morgenstern
(1902-1977)

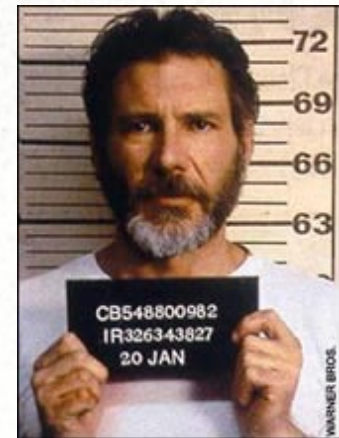


1944

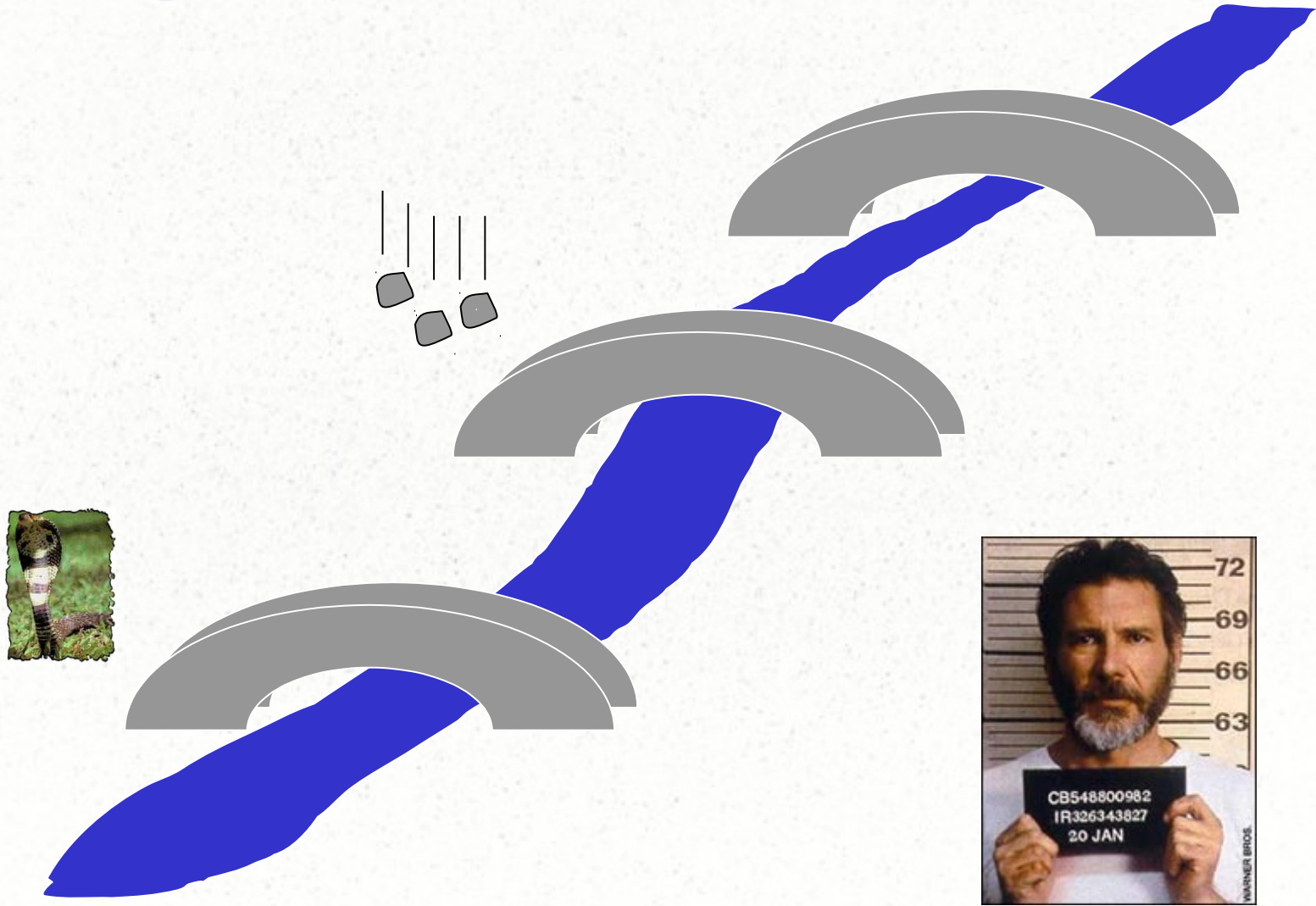
Un problema de decisión



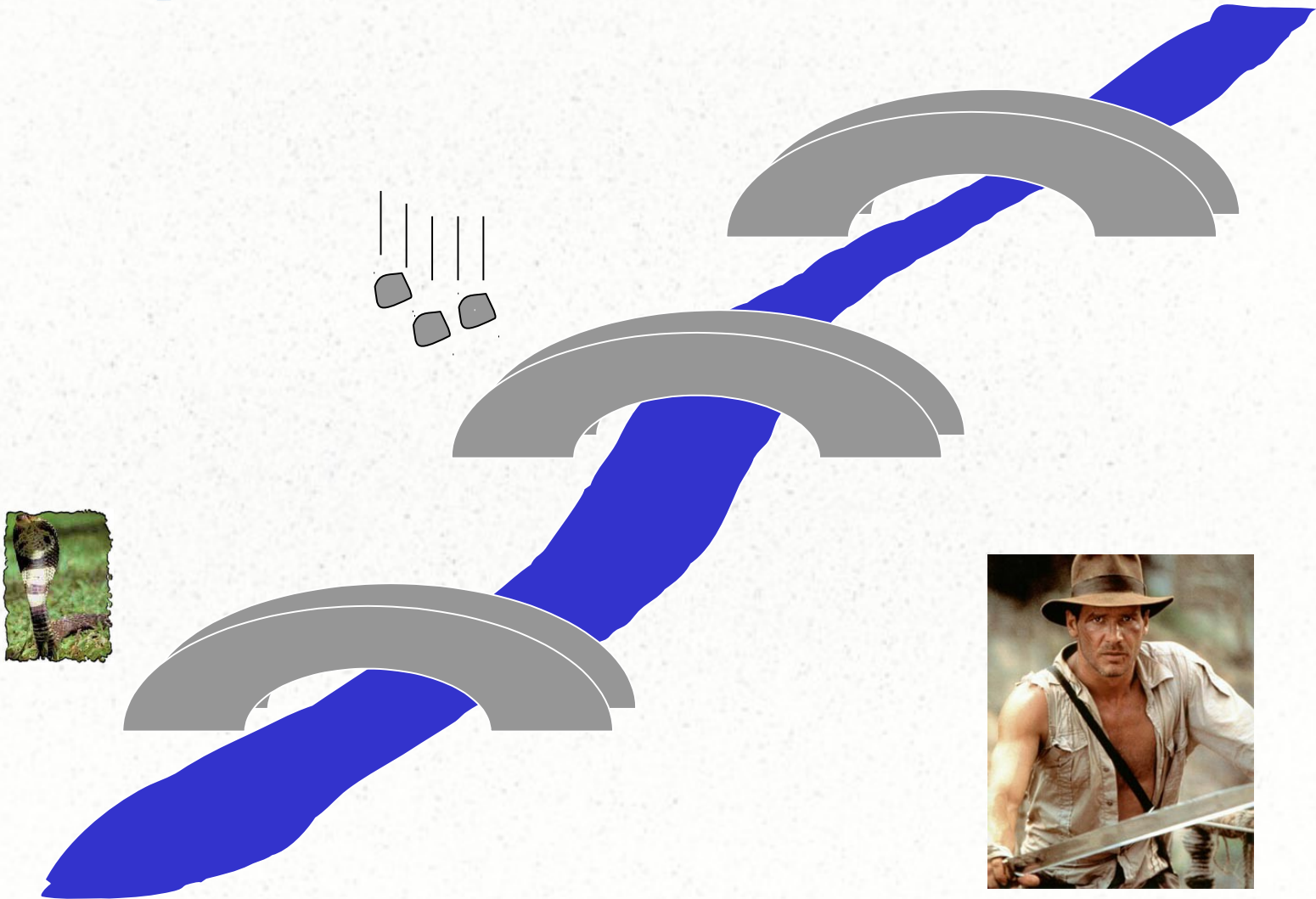
Un problema de decisión



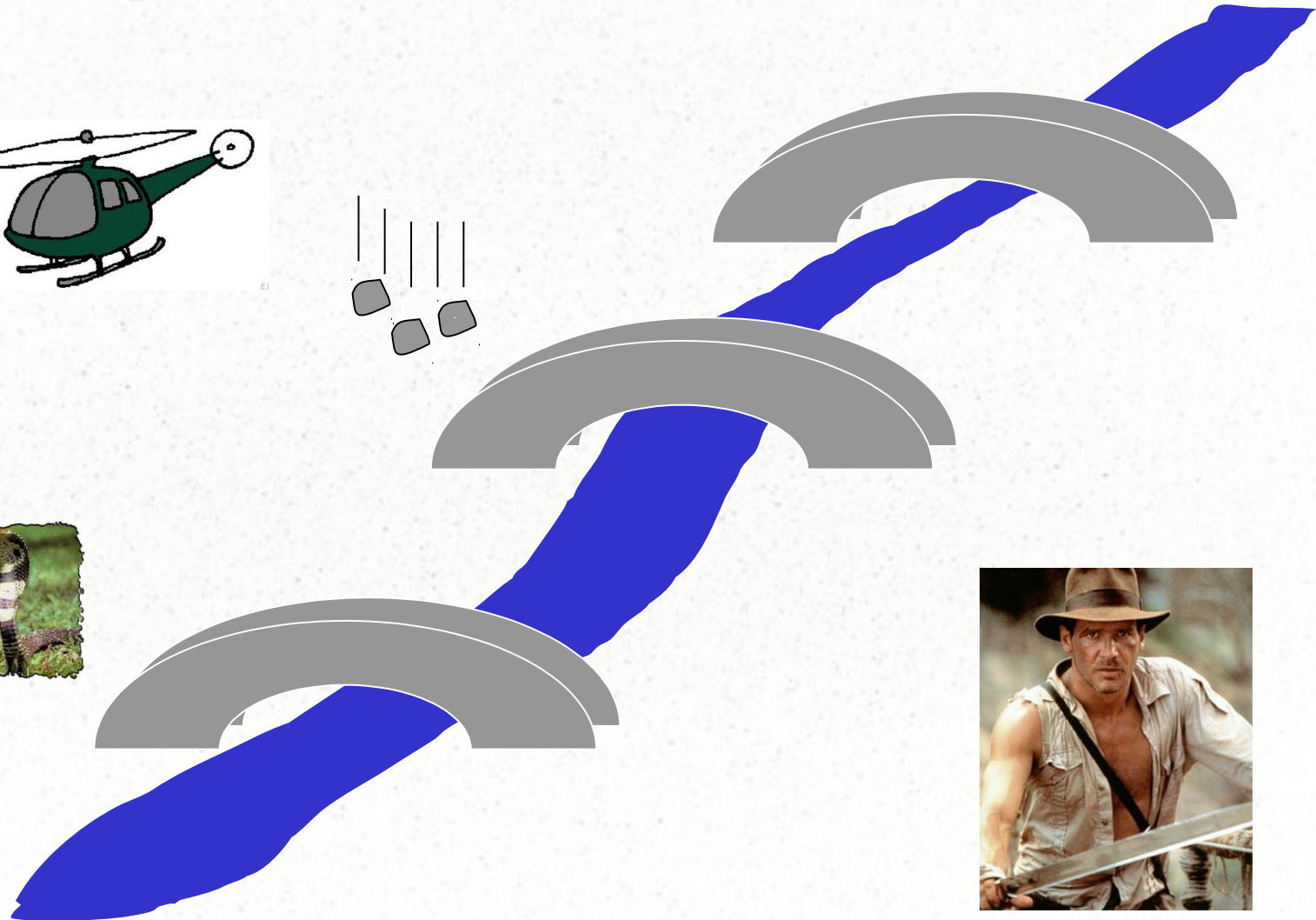
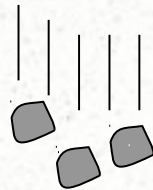
Un problema de decisión



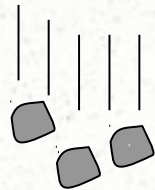
Un problema de decisión



Un problema de decisión



Un problema estratégico



Elementos de un juego

jugadores



Elementos de un juego

estrategias



Elementos de un juego

preferencias



Elementos de un juego

utilidad



0



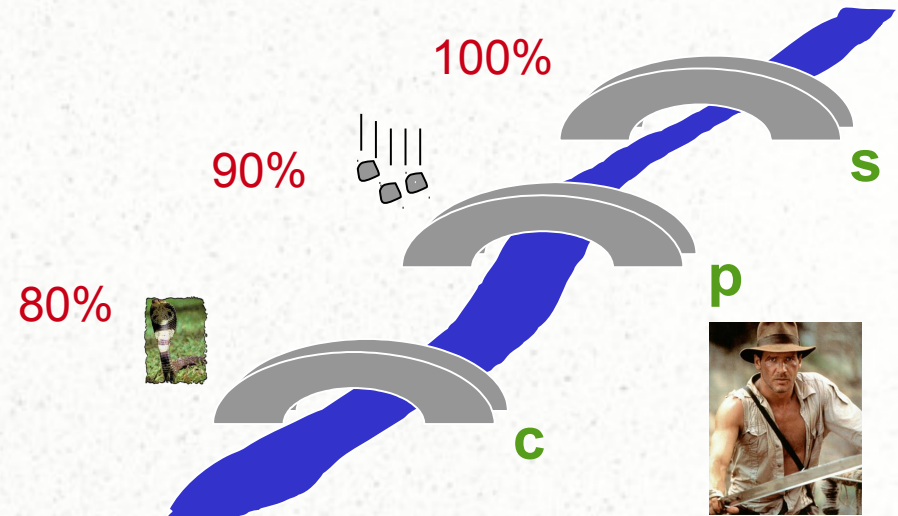
50



100

Ejemplo de utilidad

- Resultados:
vivir ($u = 1$) / morir ($u = 0$)
- Estrategias:
seguro / **p**iedras / **c**obras
- Utilidad:
 $u(\mathbf{s}) = 1.0 / u(\mathbf{p}) = 0.9 / u(\mathbf{c}) = 0.8$



Forma estratégica



	s	p	c
s	0	1	1
p	0.9	0	0.9
c	0.8	0.8	0

Forma estratégica



	s	p	c
s	1	0	0
p	0.1	1	0.1
c	0.2	0.2	1

Principio de racionalidad

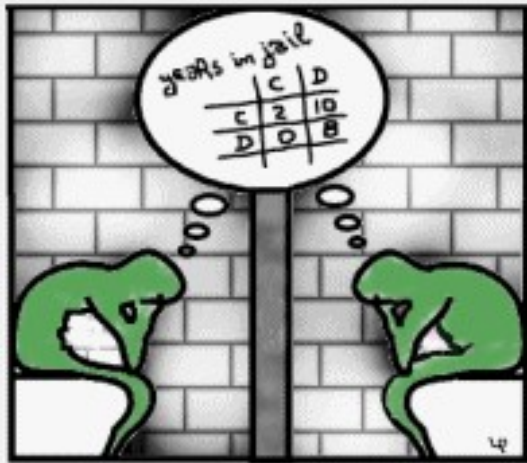
**El objetivo de todo jugador
es maximizar su utilidad**

Conocimiento común



Juegos clásicos

dilema del prisionero



prisionero 1

prisionero 2

	coop.	traic.
coop.	3	0
traic.	4	1

Juegos clásicos

piedra, papel, tijeras



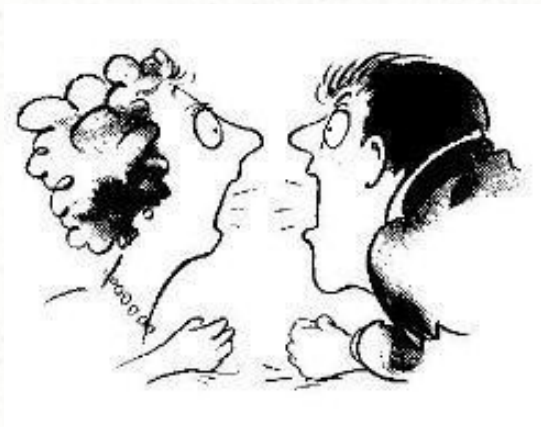
jugador 1

jugador 2

	pi	pa	ti
pi	0	-1	1
pa	1	0	-1
ti	-1	1	0

Juegos clásicos

la batalla de los sexos

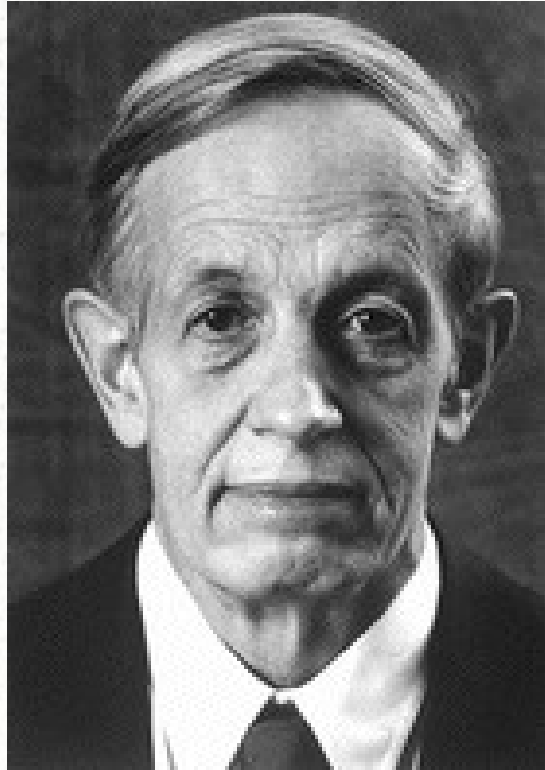


ELLA

ÉL

	ópera	fútbol
ópera	1 / 2	0 / 0
fútbol	0 / 0	2 / 1

Equilibrio de Nash



Nash (1928-)

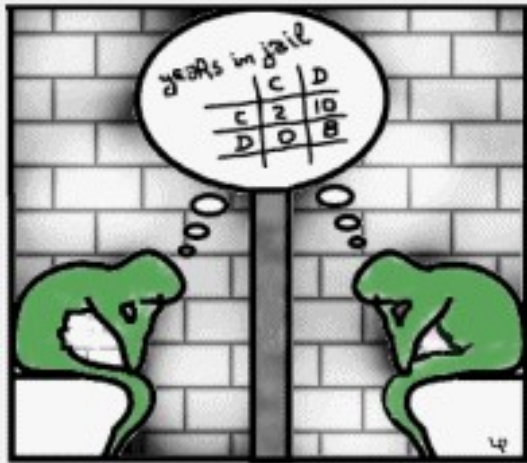
tesis de máster: 1949 - premio Nobel de Economía: 1994

Equilibrio de Nash

Una elección de estrategias de los jugadores es **equilibrio de Nash** si ninguno puede mejorar su ganancia cambiando unilateralmente de estrategia

Equilibrio único

dilema del prisionero



prisionero 1

prisionero 2

	coop.	traic.
coop.	3	0
traic.	4	1

Sin equilibrio

piedra, papel, tijeras



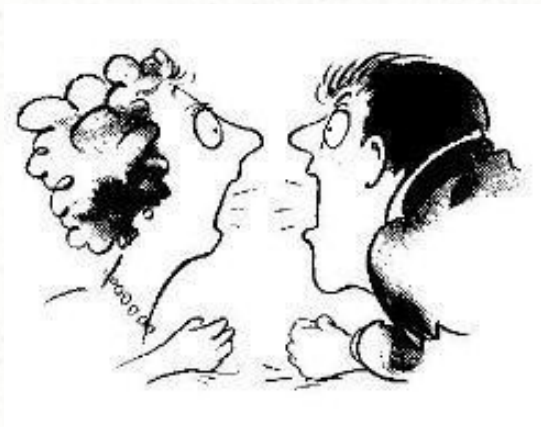
jugador 1

jugador 2

	pi	pa	ti
pi	0	-1	1
pa	1	0	-1
ti	-1	1	0

Varios equilibrios

la batalla de los sexos



ELLA

ÉL

	ópera	fútbol
ópera	1 / 2	0 / 0
fútbol	0 / 0	2 / 1

Estrategias mixtas

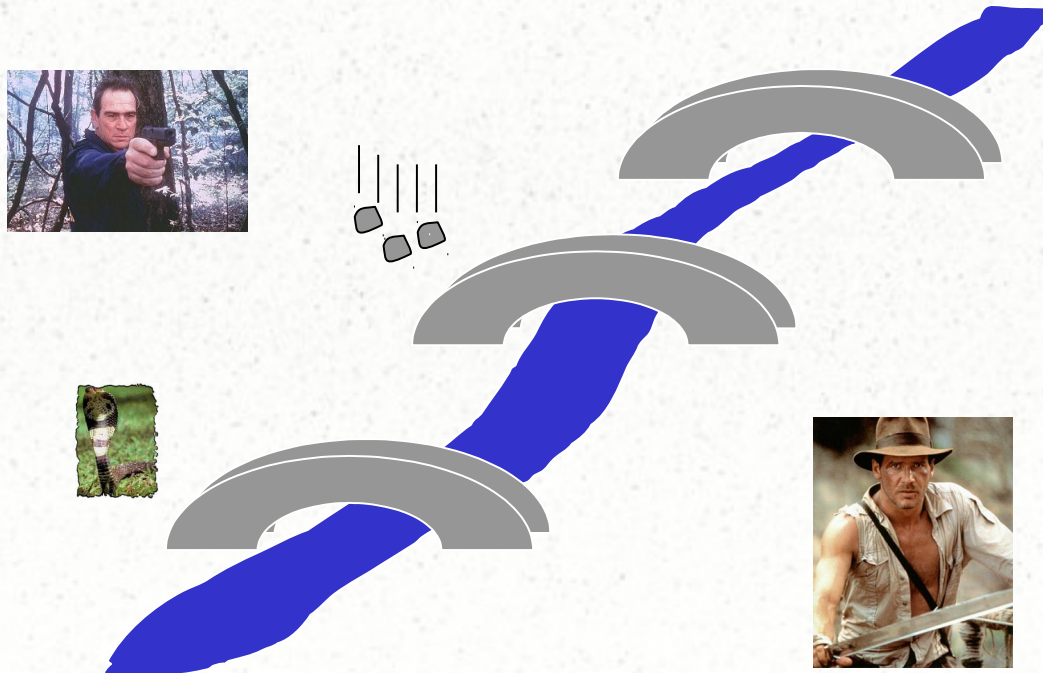
- Se elige cada estrategia pura con una probabilidad.
- Cada asignación de probabilidades es una **estrategia mixta**.



$$p(\text{piedra}) = p(\text{papel}) = p(\text{tijeras}) = 1/3$$

Equilibrio mixto

- Asignación de probabilidades que haga indiferente la elección del contrario.



Equilibrio mixto

B



A



	s	p	c
s	1	0	0
p	0.1	1	0.1
c	0.2	0.2	1

$$u_B(s) = 1.0 \times p_A(s) + 0.1 \times p_A(p) + 0.2 \times p_A(c)$$

$$u_B(p) = 0.0 \times p_A(s) + 1.0 \times p_A(p) + 0.2 \times p_A(c)$$

$$u_B(c) = 0.0 \times p_A(s) + 0.1 \times p_A(p) + 1.0 \times p_A(c)$$

$$u_B(s) = u_B(p) = u_B(c)$$

$$p_A(s) + p_A(p) + p_A(c) = 1$$

$$p_A(s) = 0.30$$

$$p_A(p) = 0.33$$

$$p_A(c) = 0.37$$

Equilibrio mixto

B



$$u_A(s) = 0.0 \times p_B(s) + 1.0 \times p_B(p) + 1.0 \times p_B(c)$$

A



	s	p	c
s	0	1	1
p	0.9	0	0.9
c	0.8	0.8	0

$$u_A(p) = 0.9 \times p_B(s) + 0.0 \times p_B(p) + 0.9 \times p_B(c)$$

$$u_A(c) = 0.8 \times p_B(s) + 0.8 \times p_B(p) + 0.0 \times p_B(c)$$

$$u_A(s) = u_A(p) = u_A(c)$$

$$p_B(s) + p_B(p) + p_B(c) = 1$$

$$p_B(s) = 0.40$$

$$p_B(p) = 0.34$$

$$p_B(c) = 0.26$$

La evolución como un juego

“La lógica del conflicto animal”



Maynard Smith
(1920-2004)



Price
(1922-1975)

NATURE VOL. 246 NOVEMBER 2 1973

The Logic of Animal Conflict

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Conflicts between animals of the same species usually are of “limited war” type, not causing serious injury. This is often explained as due to group or species selection for behaviour benefiting the species rather than individuals. Game theory and computer simulation analyses show, however, that a “limited war” strategy benefits individual animals as well as the species.

In a typical combat between two male animals of the same species, the winner gains mates, dominance rights, deniable territory, or other advantages that will tend toward transmitting its genes to future generations at higher frequency than the loser's genes. Consequently, one might expect that natural selection would develop maximally effective weapons and fighting styles for a “total war” strategy of battles between males to the death. But instead, intraspecific conflicts are usually of a “limited war” type, involving inefficient weapons or ritualized tactics that seldom cause serious injury to either contestant. For example, in wild male quails the males fight each other by venting, without using their fringes¹. In male deer (*Odocoileus hemionus*) the bucks frequently but harmlessly by craning or pushing antlers against antlers, while they refrain from attacking when an opponent turns away, exposing its unprotected side of its body². And in the Arabian oryx (*Oryx capensis*) the extremely long, backward-pointing horns are so inefficient for combat that in order for two males to fight they are forced to kneel down with their heads between their knees to direct their horns forward³. For additional examples, see Collier⁴, Darwin⁵, Hapgood⁶, Huxley *et al.*⁷, Lorenz⁸ and Wynne-Edwards⁹.

Here one can explain such oddities in males that struggle with each other, deer that refuse to strike “foal blows”, and antelope that kneel down to fight. The accepted explanation for the conventional nature of combat is that if no conventional methods existed, many individuals would be injured, and this would militate against the survival of the species (see, for example, Huxley⁵). The difficulty with this type of explanation is that it appears to assume the operation of “group selection”. Although we cannot rule out group selection as an agent producing adaptations, it is only likely to be effective in rather special circumstances^{10,11}. Consequently it seems to us that group selection cannot by itself account for the complex, consistent and behavioural adaptations for limited combat found in so many species, but there must also be individual selection for those, which means that a “limited war” strategy must be differentially advantageous for individuals.

We consider simple formal models of conflict situations,

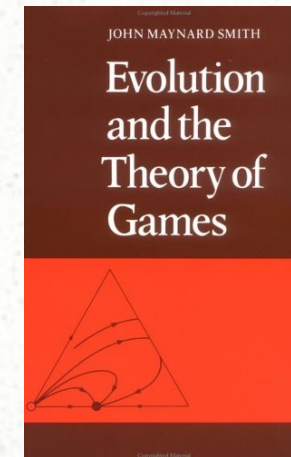
and ask what strategy will be favoured under individual selection. We first consider conflict in species possessing offensive weapons capable of inflicting serious injury on other members of the species. Then we consider conflict in species where serious injury is impossible, so that victory goes to the contestant who fights longest. For each model, we seek a strategy that will be stable under natural selection; that is, we seek an “evolutionarily stable strategy” or ESS. The concept of an ESS is fundamental to our argument; it has been derived in part from the theory of games, and in part from the work of MacArthur¹² and of Hamilton¹³ on the evolution of the sex ratio. Roughly, an ESS is a strategy such that, if most of the members of a population adopt it, there is no “mutant” strategy that would give higher reproductive fitness.

A Computer Model

A main reason for using computer simulation was to test whether it is possible even in theory for individual selection to account for “limited war” behaviour. We consider a species that possesses offensive weapons capable of inflicting serious injuries. We assume that there are two categories of conflict tactics: “conventional” tactics, which are unlikely to cause serious injury, and “dangerous” tactics, which are likely to cause serious injury if they are employed for long. (Thus in the model example, venting between C tactics and use of fringes would be D tactics. In many species, C tactics are limited to threat displays at a distance, without any physical fighting. We consider a conflict between two individuals to consist of a series of “moves”.) At each move, a contestant can employ C or D tactics, or retreat. If a contestant employs D tactics, there is a fixed probability that his opponent will seriously injure a contestant who is seriously injured always retreats. If a contestant retreats, the contest is at an end and his opponent is the winner. A possible conflict between contestants A and B can be represented in this way:

A's move CCCCCCCCCCCCCCCCCC
B's move CCCCCCCCCCCCCCCCCC
If a contestant plays D on the first move of a contest, or plays D in response to C by his opponent, this is called a “probe” or a “provocation”. A probe made after the opening move is said to be “retaliated”, a contest from C to D level. A contestant who plays D in reply to a probe is said to “retaliate”. In the example shown above, A probes on his twelfth and twentieth moves; B retaliates after the first probe, but retreats after the second, leaving A the winner. At the end of a contest there are “pay-offs” to each contestant. The pay-offs are taken as measures of the contribution the contest has made to the reproductive success of the individual. They take account of these factors: the advantage of winning as compared with losing; the disadvantage of being seriously injured; and the disadvantage of wasting time and energy in the contest.

15



1982



Nature, 1973

Teoría de Juegos evolutiva

	TJ clásica	TJ evolutiva
jugadores	racionales	irracionales
estrategias	elegibles	heredadas (fenotipos)
interacción	todos a la vez	muestreo aleatorio de una población
resultados	utilidad	capacidad reproductiva (<i>fitness</i>)

Halcones y palomas



R = recurso (comida)

D = daño recibido en conflicto

individuo 2

$D > R$

individuo 1

	halcón	paloma
halcón	$(R-D)/2$	R
paloma	0	$R/2$

Halcones y palomas



R = recurso (comida)

D = daño recibido en conflicto

individuo 2

$D > R$

individuo 1

	halcón	paloma
halcón	$(R-D)/2$	R
paloma	0	$R/2$

Halcones y palomas

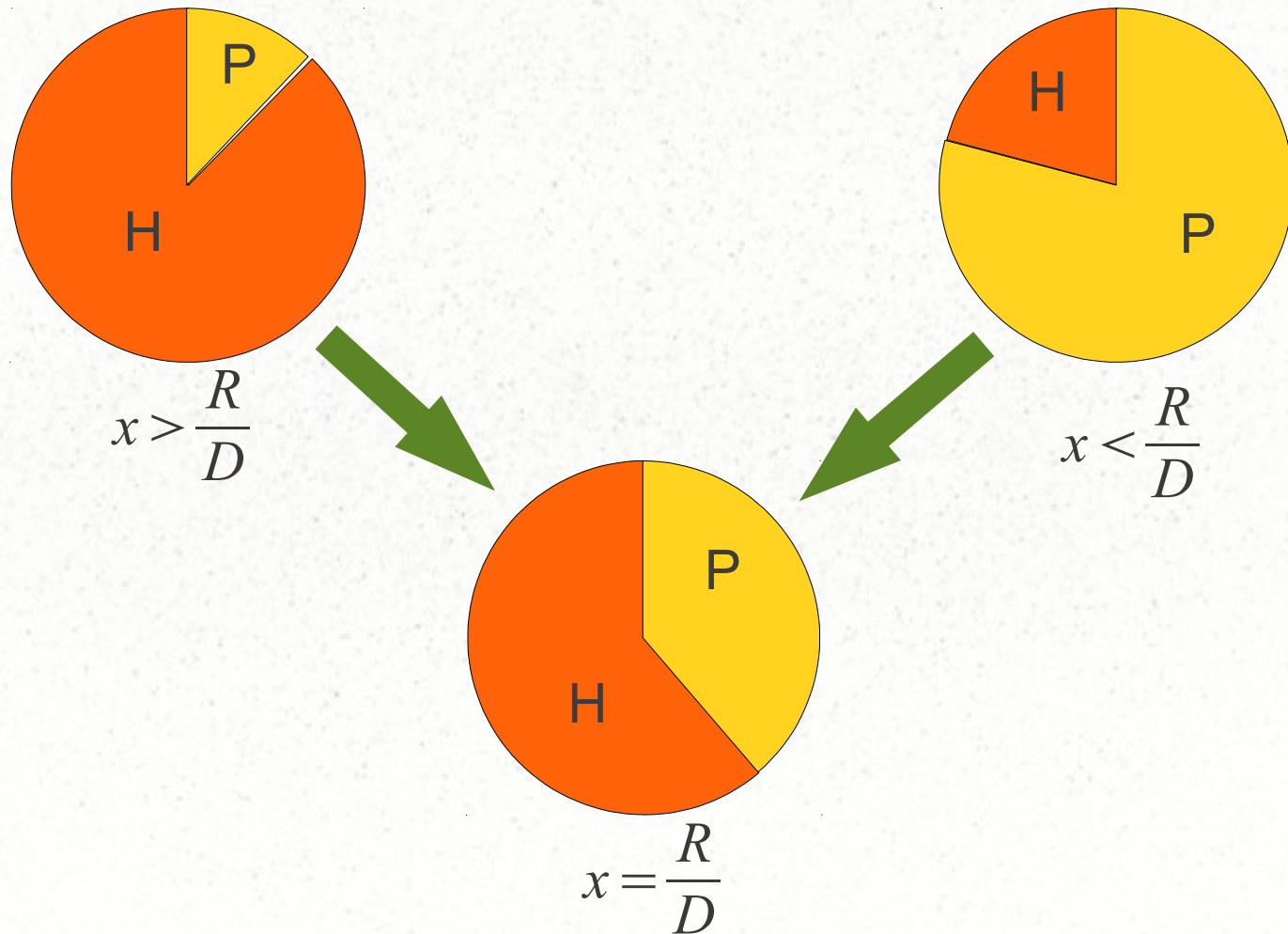
x = fracción de halcones

$$f_H(x) = \frac{R-D}{2}x + R(1-x)$$

$$f_P(x) = \frac{R}{2}(1-x)$$

$$f_H(x) - f_P(x) = \frac{R-D}{2}x \quad \begin{cases} f_H(x) > f_P(x) & \text{si } x < \frac{R}{D} \\ f_H(x) < f_P(x) & \text{si } x > \frac{R}{D} \end{cases}$$

Estrategia Evolutivamente Estable



Ecuación del replicador

$$\frac{d x_i}{d t} = x_i [f_i(\mathbf{x}) - \bar{f}(\mathbf{x})]$$

- Equilibrios de Nash mixtos = Puntos fijos de la ecuación del replicador
- Puntos fijos atractores = Estrategias Evolutivamente Estables

Ejemplos

Demostraciones de fuerza



¿Por qué hay tantos machos como hembras?



***¿Por qué hay tantos machos
como hembras?***



¿Por qué hay tantos machos como hembras?



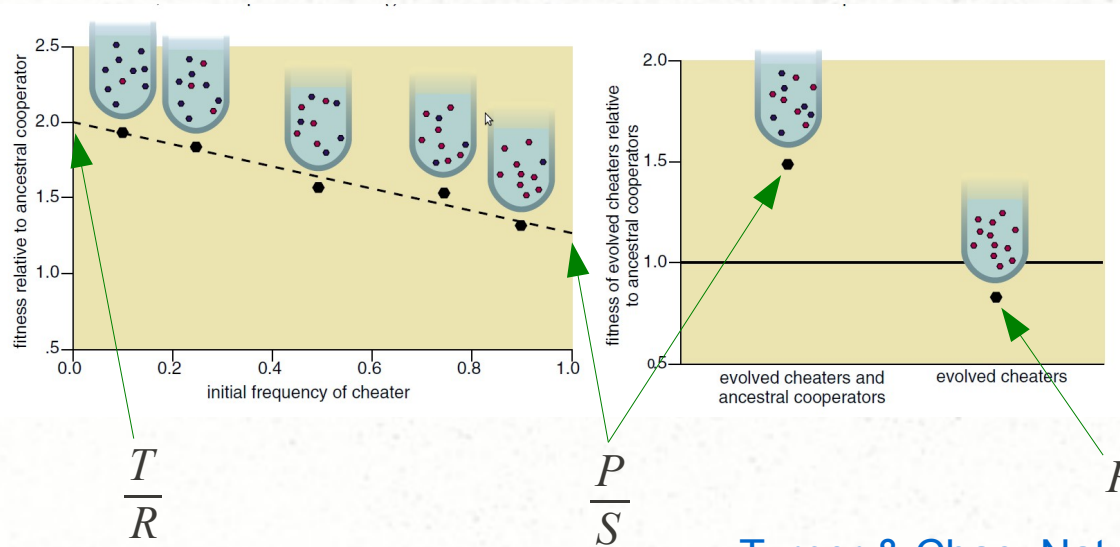
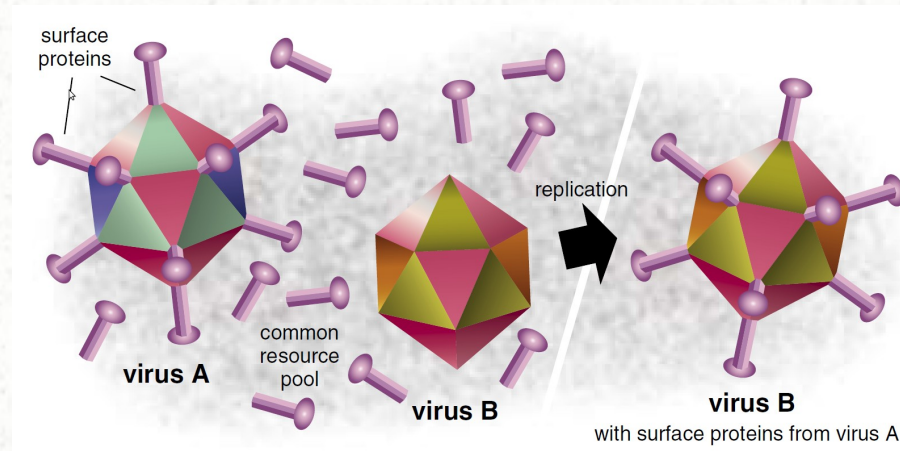
si hay más machos, ten hijas...



si hay más hembras, ten hijos...

...y tendrás más nietos

Parásitos de parásitos

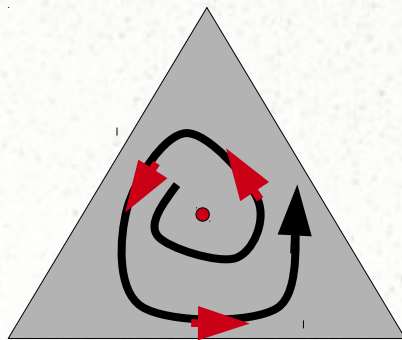


	cooperator	cheater
cooperator	 reward $R = 1$	 sucker's payoff $S = 1 - s_1$
cheater	 temptation to cheat $T = 1 + s_2$	 punishment $P = 1 - c$

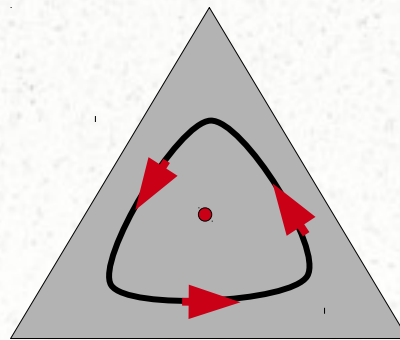
Turner & Chao, Nature **398**, 441-443 (1999)

Piedra-papel-tijeras

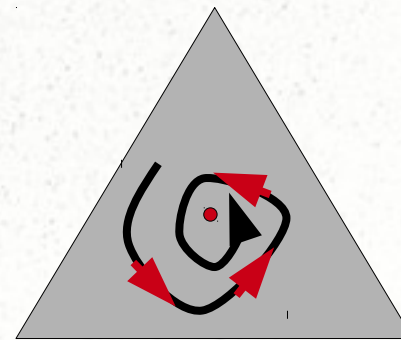
$$W = \begin{pmatrix} \text{Pi} & \text{Pa} & \text{Ti} \\ 0 & -a_2 & b_3 \\ b_1 & 0 & -a_3 \\ -a_1 & b_2 & 0 \end{pmatrix} \begin{matrix} \text{Pi} \\ \text{Pa} \\ \text{Ti} \end{matrix}$$



$$|W| < 0 \\ (a_1 a_2 a_3 > b_1 b_2 b_3)$$



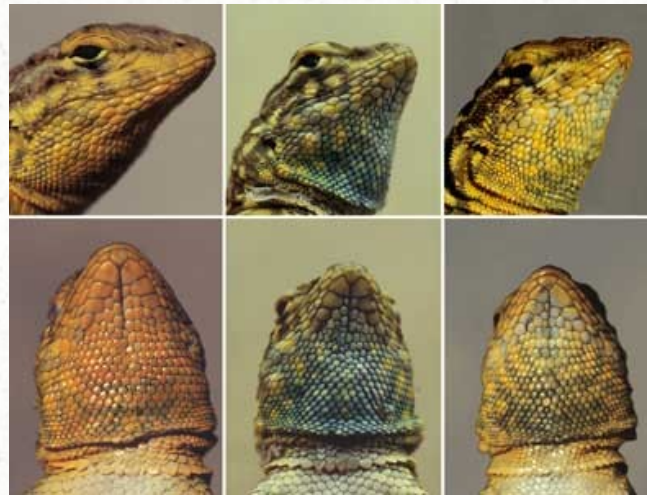
$$|W| = 0 \\ (a_1 a_2 a_3 = b_1 b_2 b_3)$$



$$|W| > 0 \\ (a_1 a_2 a_3 < b_1 b_2 b_3)$$

Piedra-papel-tijeras

Uta stansburiana

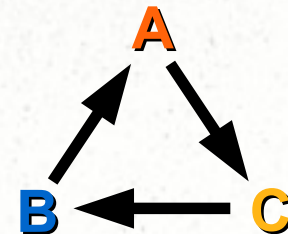


A

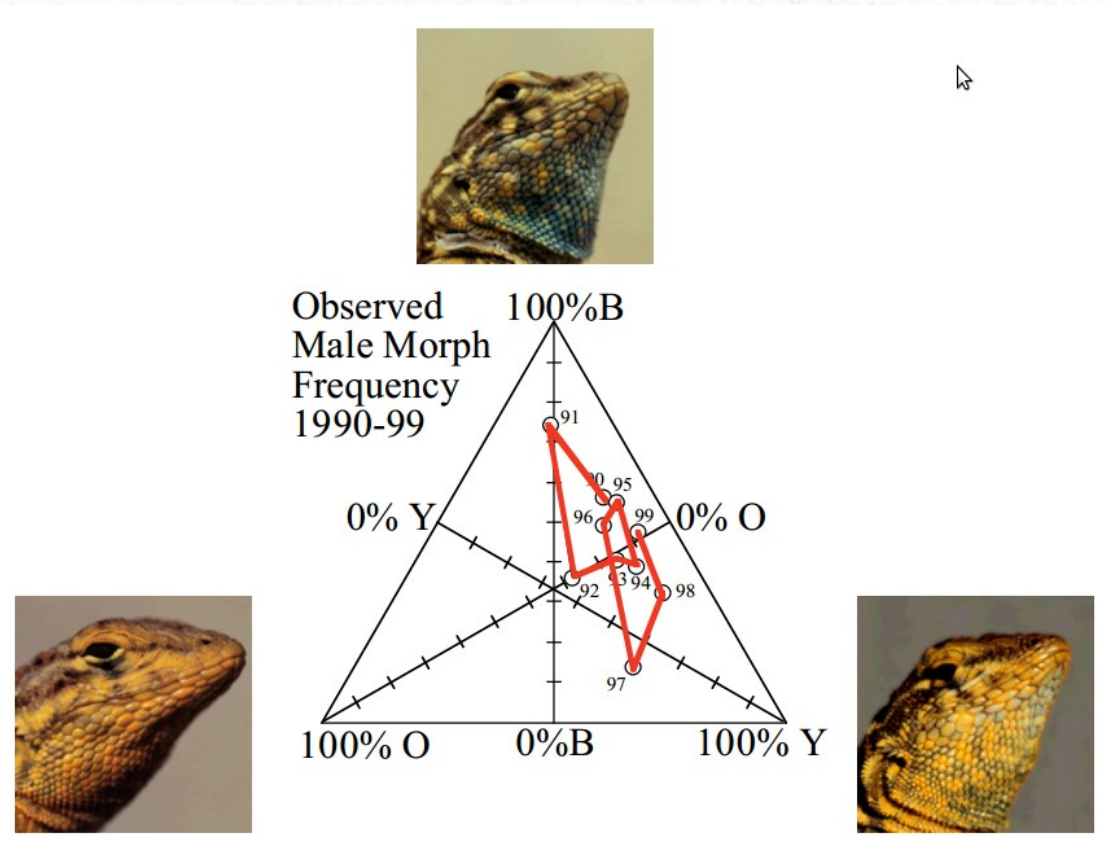
B

C

- A** monógamo y celoso
- B** polígamo y descuidado
- C** oportunista



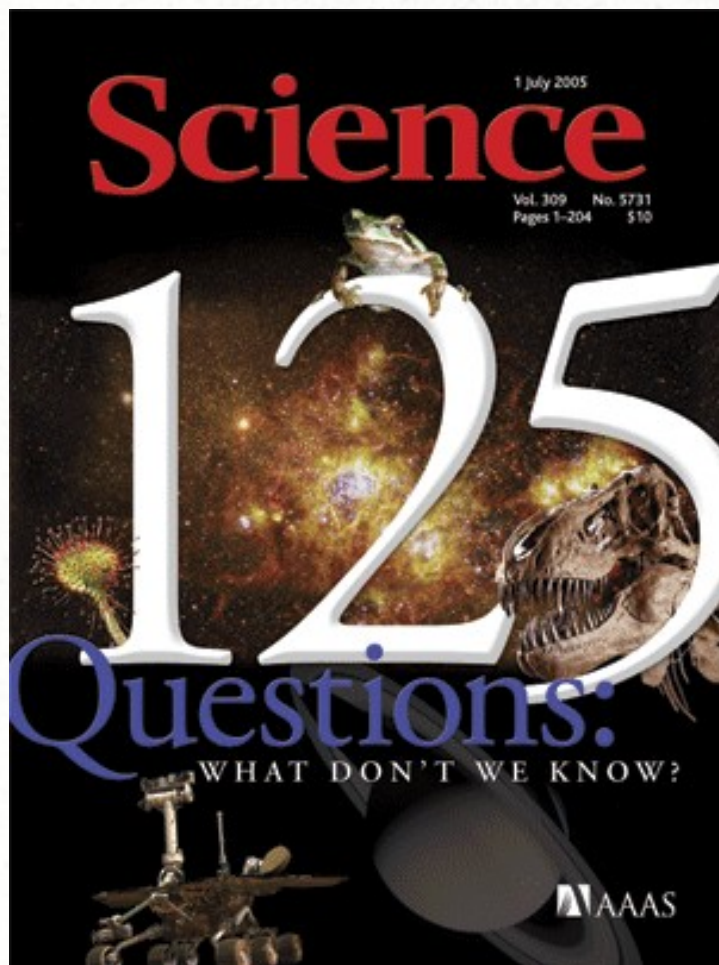
Piedra-papel-tijeras



Zamudio & Sinervo, PNAS **97**, 14427-14432 (2000)

La evolución de la cooperación

Un problema fundamental



When Charles Darwin was working out his grand theory on the origin of species, he was perplexed by the fact that animals from ants to people form social groups in which most individuals work for the common good. This is seemed to run counter to his proposal that individual fitness was key to surviving over the long term.

By the time he wrote *The Descent of Man*, however, he had come up with a few explanations. He suggested that natural selection could encourage altruistic behavior among kin so as to improve the reproductive potential of the "family." He also introduced the idea of reciprocity: that unrelated but familiar individuals would help each other out if both were altruistic. A century of work with dozens of social species has borne out his ideas to some degree, but the details of how and why cooperation evolved remain to be worked out. The answers could help explain human behaviors that seem to make little sense from a strict evolutionary perspective, such as taking one's life to save a drowning stranger.

Animals help each other out in many ways. In social species from honeybees to naked mole rats, kinship fosters cooperation. Females forgo reproduction and instead help the dominant female with her young. And common gendras help unrelated individuals work together. Male chimpanzees, for example, gang up against predators, protecting each other at a potential cost to themselves.

Generosity is pervasive among humans. Indeed, some anthropologists argue that the evolution of the tendency to trust one's relatives and neighbors

helped humans become Earth's dominant vertebrate. The ability to work together provided our early ancestors more food, better protection, and better childcare, which in turn improved reproductive success.

However, the degree of cooperation varies. "Cheaters" can gain a leg up on the rest of humankind, at least in the short term. But cooperation prevails among many species, suggesting that this behavior is a better survival strategy, over the long run, despite all the strife among ethnic, political, religious, even family groups now rampant within our species.



How Did Cooperative Behavior Evolve?

Evolutionary biologists and animal behavior researchers are searching out the genetic basis and molecular drivers of cooperative behaviors, as well as the physiological, environmental, and behavioral inputs for sociality. Neuroscientists studying mammals from voles to humans are discovering key correlations between brain chemicals and social strategies.

Others with a more mathematical bent are applying evolutionary game theory, a modeling approach developed for economics, to quantify cooperation and predict behavioral outcomes under different circumstances. Game theory has helped reveal a seemingly innate desire for fairness: Game players will spend time and energy to punish unfair actions, even though there's nothing to be gained by these actions for themselves. Sim-

ilar studies have shown that even when two people meet just once, they tend to be fair to each other. Those actions are hard to explain, as they don't seem to follow the basic tenet that cooperation is really based on self-interest.

The models developed through these games are still imperfect. They do not adequately consider, for example, the effect of emotions on cooperation. Nonetheless, with game theory's increasing sophistication, researchers hope to gain a clearer sense of the rules that govern complex societies.

Together, these efforts are helping social scientists and others build on Darwin's observations about cooperation. As Darwin predicted, reciprocity is a powerful fitness tactic. But it is not a persuasive one.

continued >>

Why do we dream?
Pread thought-forming provides a neural forerunner to conscious dreams. New, neuroscientists suspect that brain activity during REM sleep—when dreams occur—is crucial for learning. In the experience of dreamtangent, what effect?



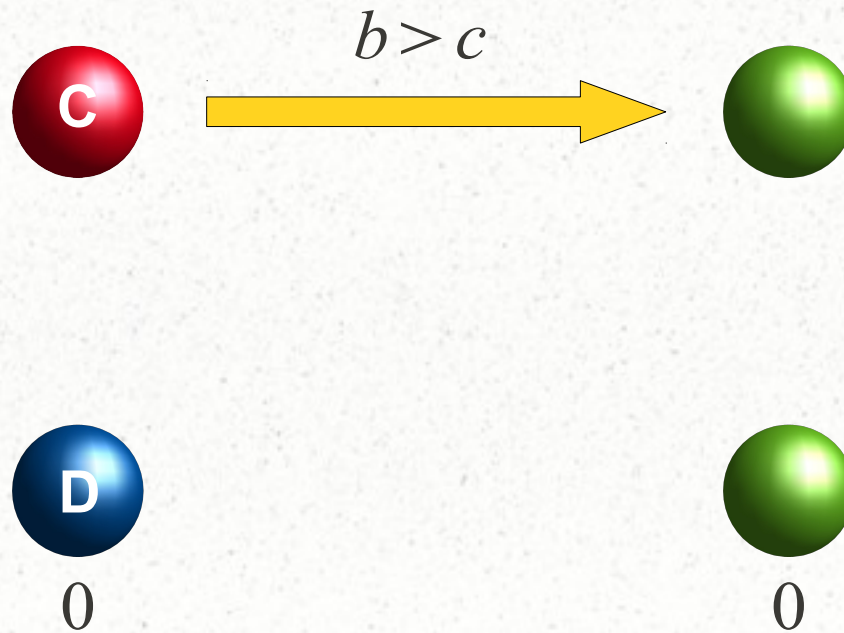
Why are there critical periods for language learning?
Monitor high-frequency in young children—including infants—may shed light on why children pick up languages so easily while adults often struggle to learn a second language in a foreign tongue.

Do pheromones influence human behavior?
Many animals use airborne chemicals to communicate, particularly when mating. Controversial studies have linked that humans to some pheromones. Identifying them will be key to assessing their role in our social lives.

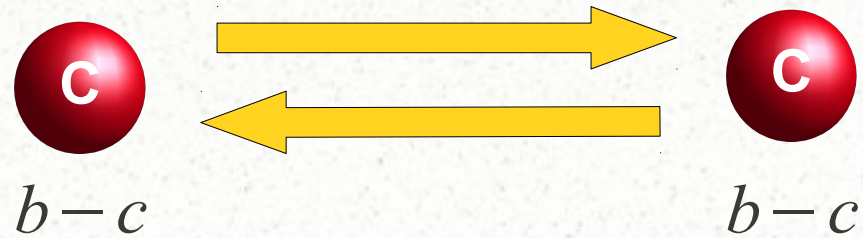


How do general anesthetics work?
Scientists are chipping away at this deep question on individual neurons, but understanding how they render an unconscious will be a long haul to crack.

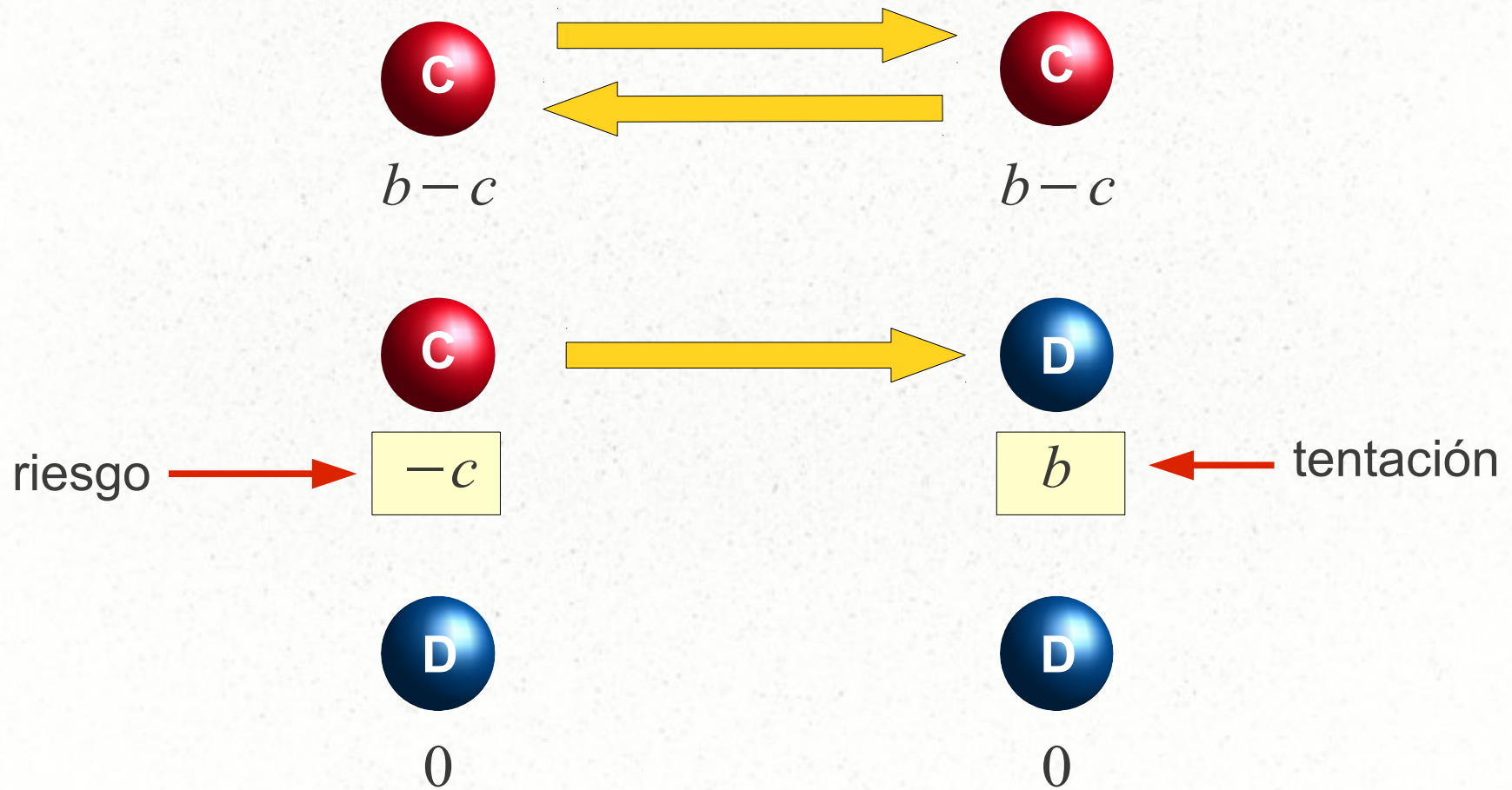
El problema



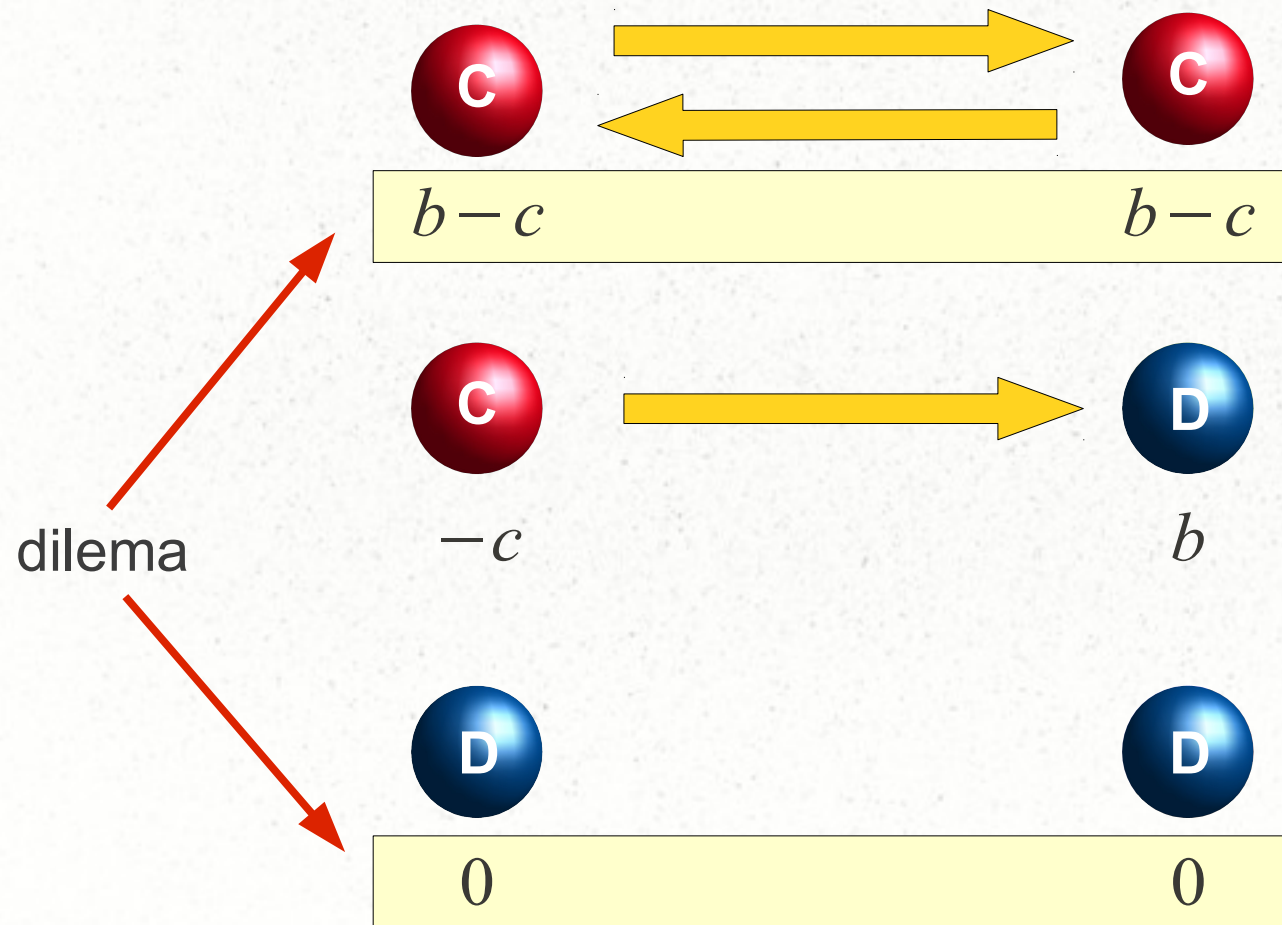
El problema



El problema



El problema

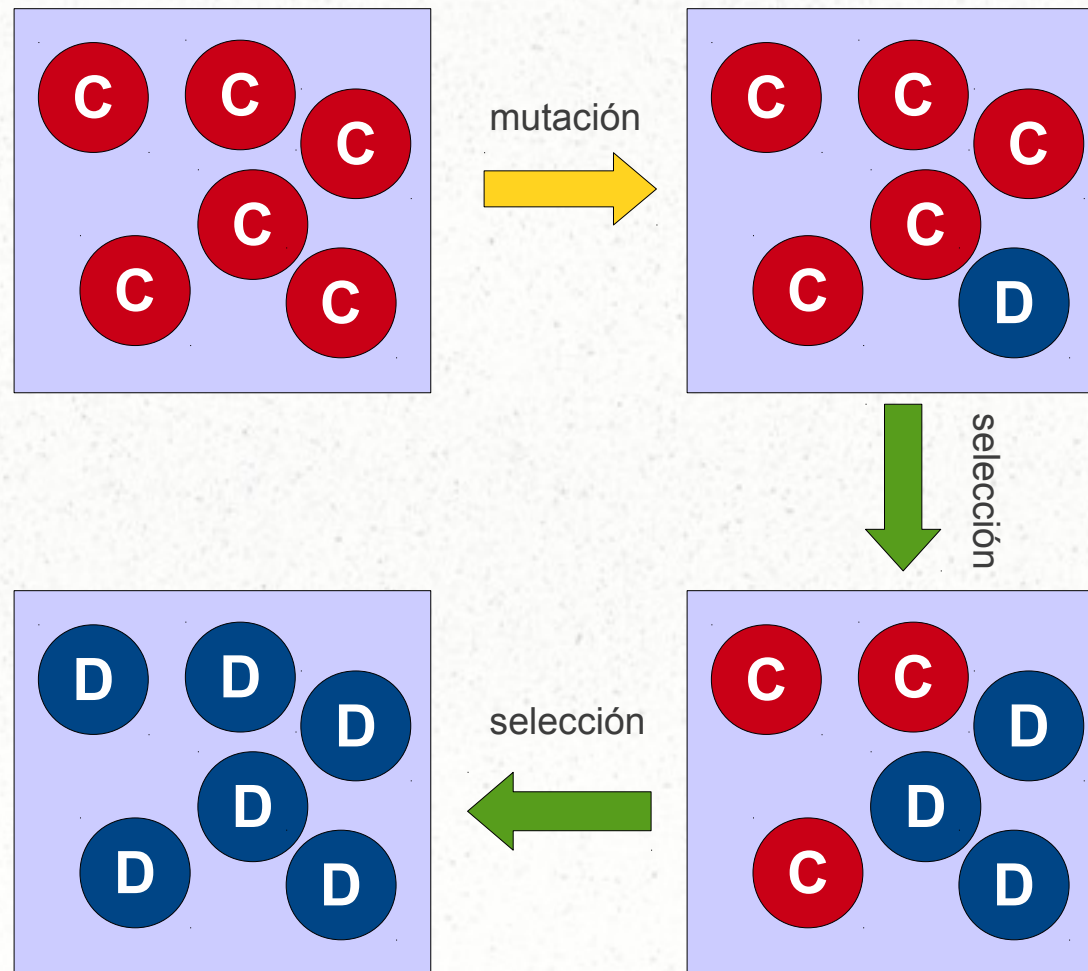


El problema

Aquél que está dispuesto a sacrificar su vida [...] a menudo no deja descendientes que hereden su noble naturaleza. [...] Por lo tanto, es sumamente improbable que el número de hombres dotados de tales virtudes [...] aumente por obra de la selección natural, es decir, por la supervivencia de los más aptos.

Charles Darwin, *El Origen del Hombre*, 1871

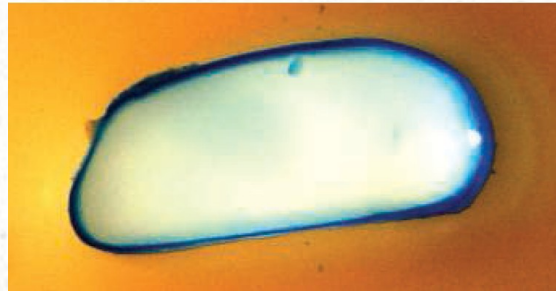
El problema



¿Por qué es un problema?



"quorum sensing"



células de levadura en etanol



hormigas



papiones

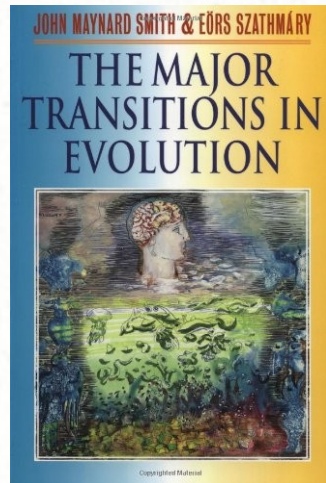


cazadores-recolectores



socorrismo

¿Por qué es tan importante?



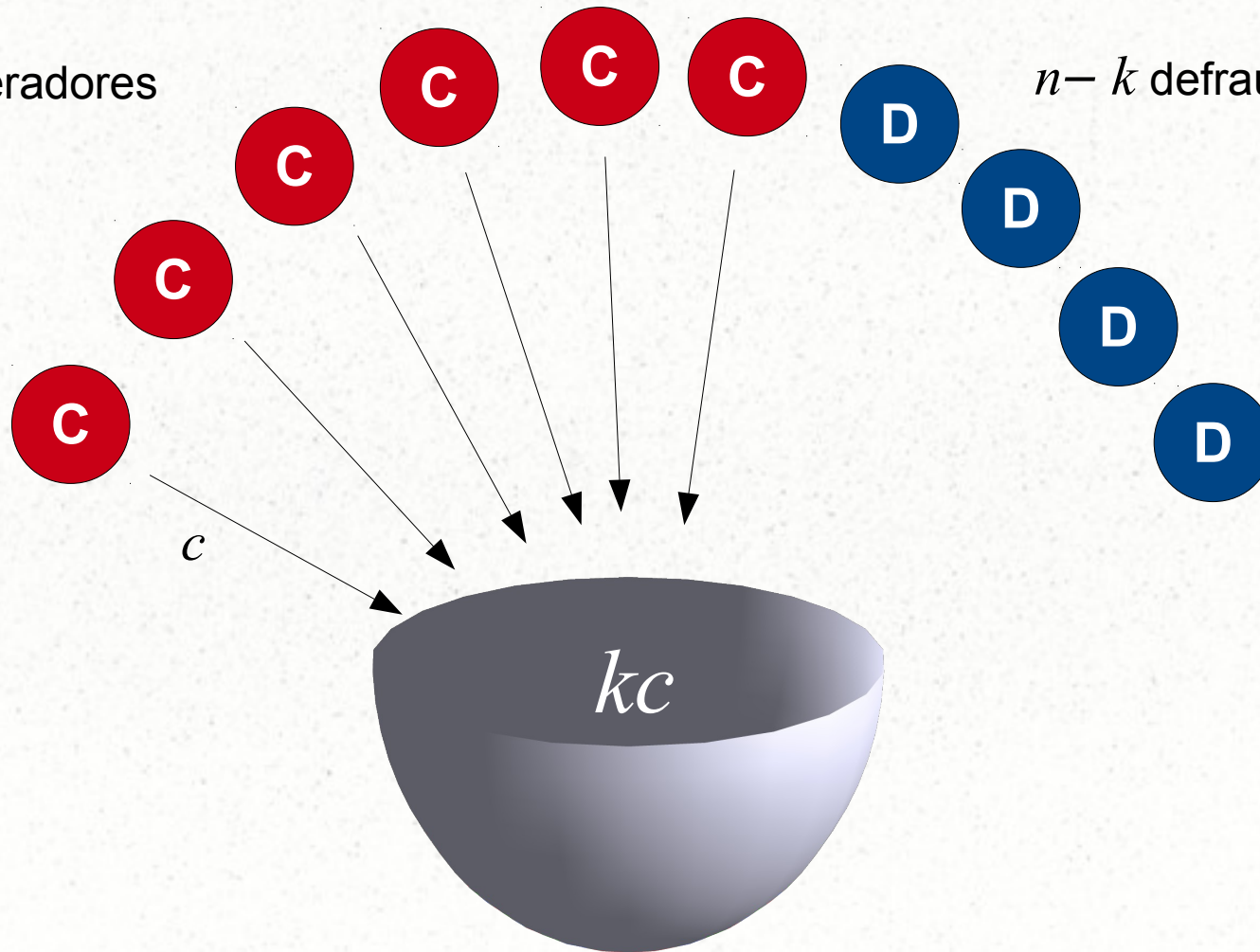
1995

moléculas replicadoras	→	poblaciones compartimentalizadas de moléculas
replicadores individuales	→	cromosomas
mundo ARN	→	ADN y proteínas (<i>código genético</i>)
procariotas	→	eucariotas
clones asexuales	→	poblaciones sexuales
organismos unicelulares	→	organismos pluricelulares (<i>diferenciación celular</i>)
individuos	→	colonias sociales (<i>castas no reproductivas</i>)
sociedades de primates	→	sociedades humanas (<i>lenguaje</i>)

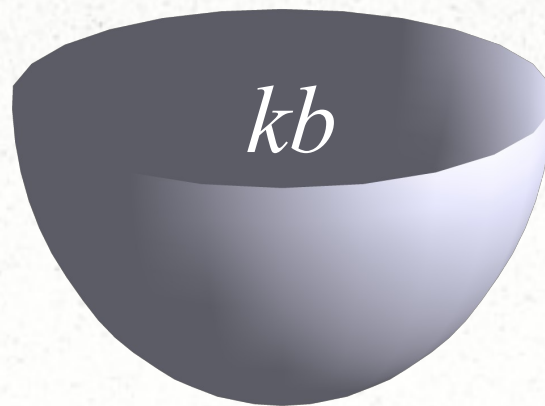
Juego de bienes públicos

k cooperadores

$n - k$ defraudadores

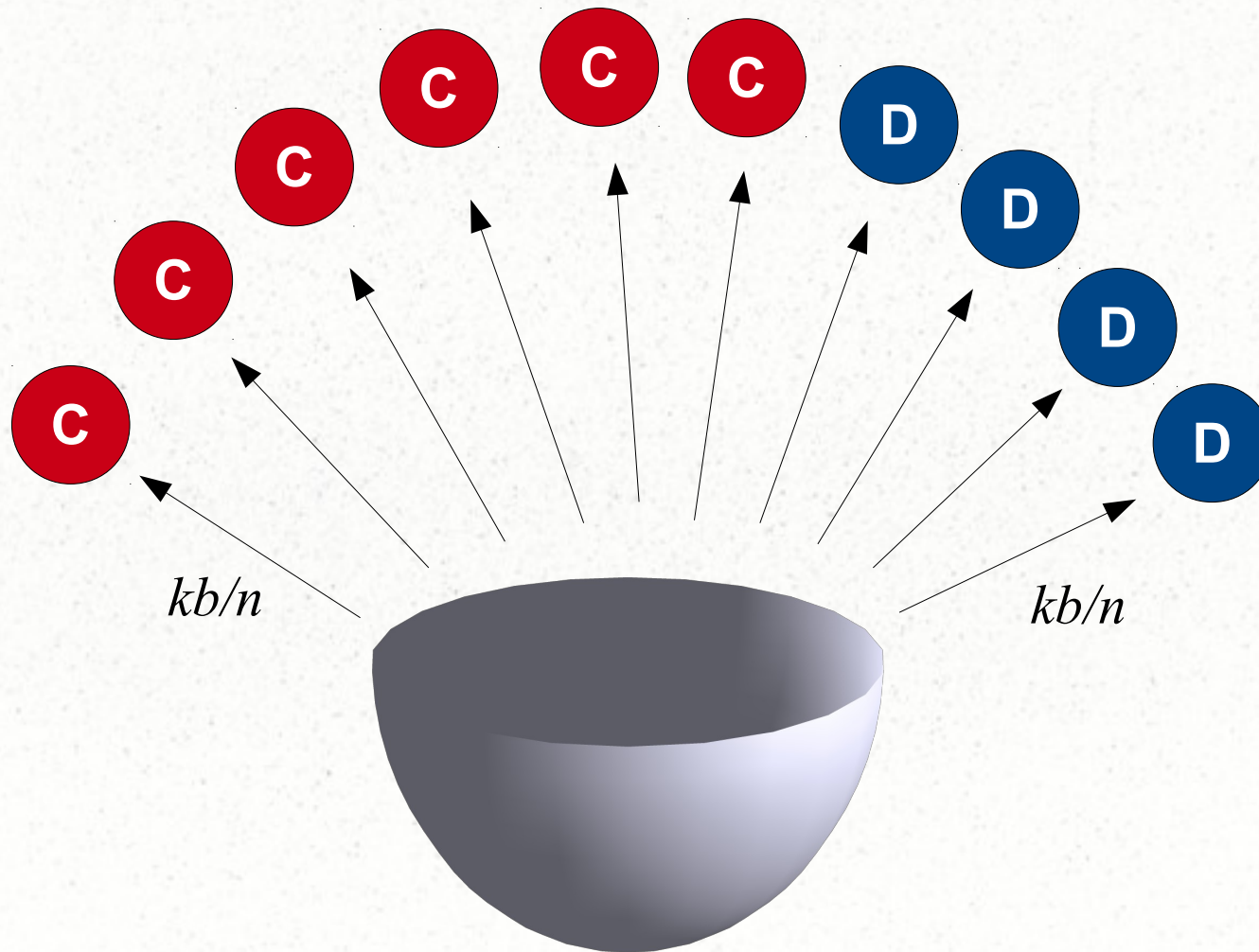


Juego de bienes públicos



$$b > c$$

Juego de bienes públicos



Juego de bienes públicos

$$G_C(k) = k \frac{b}{n} - c, \quad k = 1, \dots, n$$

$$G_D(k) = k \frac{b}{n}, \quad k = 0, \dots, n-1$$

$n=2 \rightarrow$ dilema del prisionero

Juego de bienes públicos

	propia	ajena
G_C	$\frac{b}{n} - c$	$(k-1)\frac{b}{n}$
G_D	0	$k\frac{b}{n}$

$$\frac{b}{n} - c < 0 \rightarrow \text{altruismo "fuerte"}$$

$$\frac{b}{n} - c > 0 \rightarrow \text{altruismo "débil"}$$

Una solución: segregación

	propia	ajena
G_C	$\frac{b}{n} - c$	$e_C \frac{b}{n}$
G_D	0	$e_D \frac{b}{n}$

e_C → # medio de cooperadores en torno a un cooperador

e_D → # medio de cooperadores en torno a un defraudador

Una solución: segregación

	propia	ajena
G_C	$\frac{b}{n} - c$	$e_C \frac{b}{n}$
G_D	0	$e_D \frac{b}{n}$

la cooperación prospera si

$$(e_C + 1) \frac{b}{n} - c > e_D \frac{b}{n} \quad \Leftrightarrow \quad e_C - e_D > \frac{cn}{b} - 1$$

Caso 1: población mezclada

$$e_C - e_D > \frac{cn}{b} - 1$$

- Población mezclada con fracción de cooperadores x

$$e_C = e_D = x(n-1)$$

la cooperación prospera sii $\frac{b}{n} > c$ (altruismo débil)

Caso 2: segregación total

$$e_C - e_D > \frac{cn}{b} - 1$$

- Los cooperadores solo interactúan con cooperadores
- Los defraudadores solo interactúan con defraudadores

$$e_C = n - 1 \quad e_D = 0$$

la cooperación prospera si $b > c$

Caso 3: cooperadores aislados

$$e_C - e_D > \frac{cn}{b} - 1$$

- Cada grupo solo contiene 1 cooperador

$$e_C = 0 \quad e_D = 1$$

la cooperación no prospera

Regla de Hamilton

$$r b > c, \quad r = \frac{e_C - e_D + 1}{n}$$

- Hamilton (1964) llamó a r “parentesco”
- Segregación extrema: $r = 1$
- Cooperadores aislados: $r = 0$

Cambio de pregunta

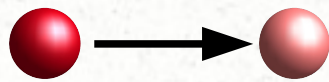
¿por qué emerge la cooperación?



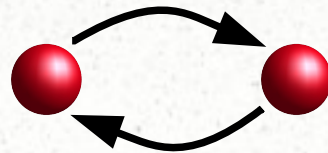
¿cómo se segregan los cooperadores?

Mecanismos de segregación

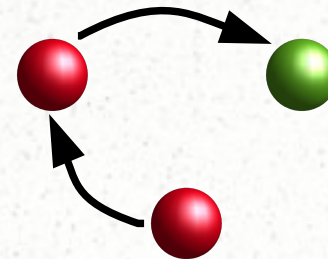
Nowak, Science (2006) 314, 1560–1563



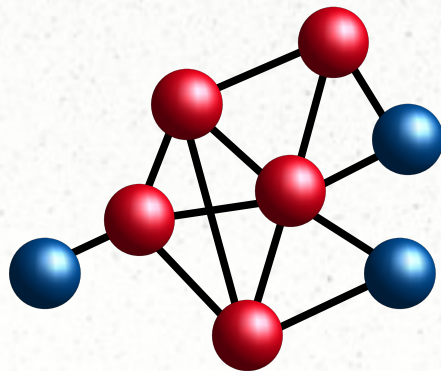
selección por
parentesco



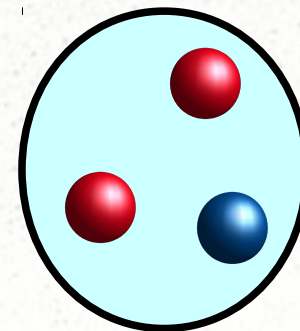
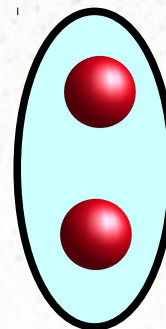
reciprocidad directa



reciprocidad indirecta

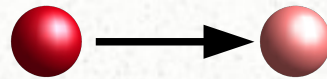


estructura de la población



selección de grupos

Selección por parentesco



«¿Que si daría mi vida por un hermano? No, pero sí por dos hermanos o por ocho primos»

John B. S. Haldane

Hamilton's rule:

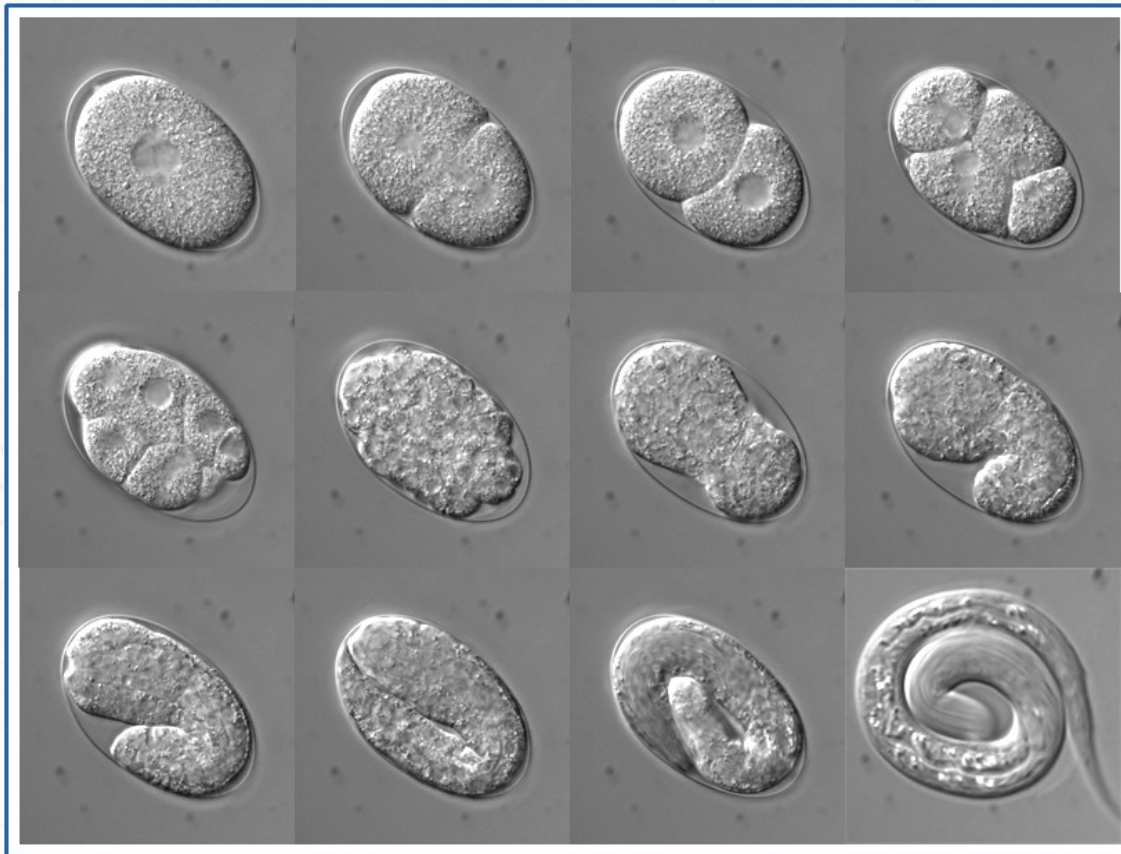
$$r b > c$$

parentesco { hermanos: $r = 1/2$
primos: $r = 1/8$

Insectos sociales

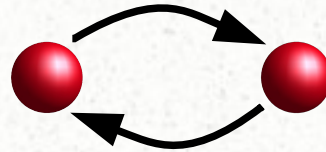


Organismos pluricelulares



Caenorhabditis elegans

Reciprocidad directa



dilema del prisionero iterado: se repite el juego con probabilidad w

vengativo	→	C C C ... C C D D ... D ...
contrincante	→	C C C ... C D X X ... X ...
		(n)

$$\left. \begin{aligned} G(D_n) &= \frac{1-w^n}{1-w}(b-c) + b w^n \\ G(D_\infty) &= \frac{1}{1-w}(b-c) \end{aligned} \right\} G(D_\infty) - G(D_n) = w^n \frac{wb-c}{1-w}$$

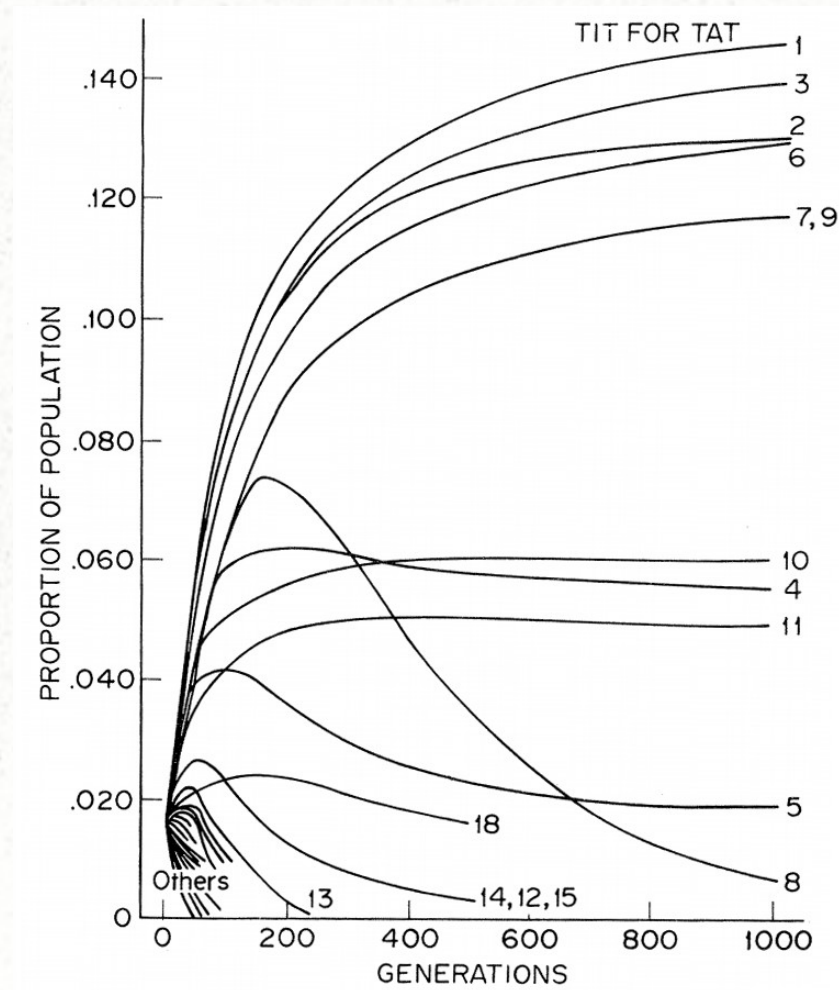
$$wb > c$$

Los torneos de Axelrod

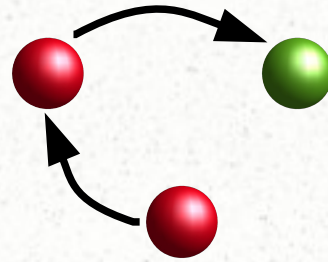
Axelrod (1984) *The evolution of cooperation* (Basic Books)

- 13 (primer torneo) y 62 (segundo torneo) estrategias, más RANDOM, jugaban 200 iteraciones del DP iterado
- Ganador absoluto: Tit-for-tat (TFT; “ojo por ojo”), de Rapoport:
 - Empieza cooperando
 - Hace lo que el oponente le hizo en la ronda anterior
- Las mejores estrategias son:
 - **Amables**: empiezan cooperando
 - **Susceptibles**: se vengan tras una decepción
 - **Compasivas**: ayudan a restaurar la cooperación
 - **Simples**: su comportamiento es fácil de entender

Los torneos de Axelrod



Reciprocidad indirecta



- Segregación conseguida a través de “señales”
- Problema: señales falsas



serpiente de coral oriental
(venenosa)



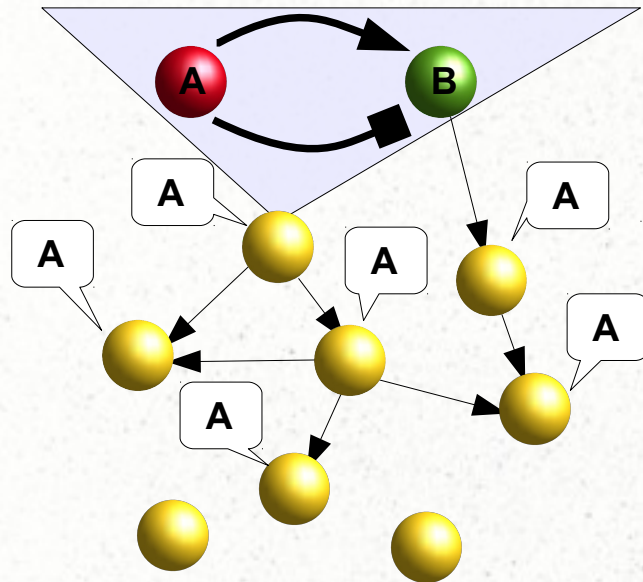
falsa serpiente de coral
(no venenosa)

Señales costosas

principio del “hándicap” (Zahavi)



Reputación



q → probabilidad de conocer la reputación del oponente

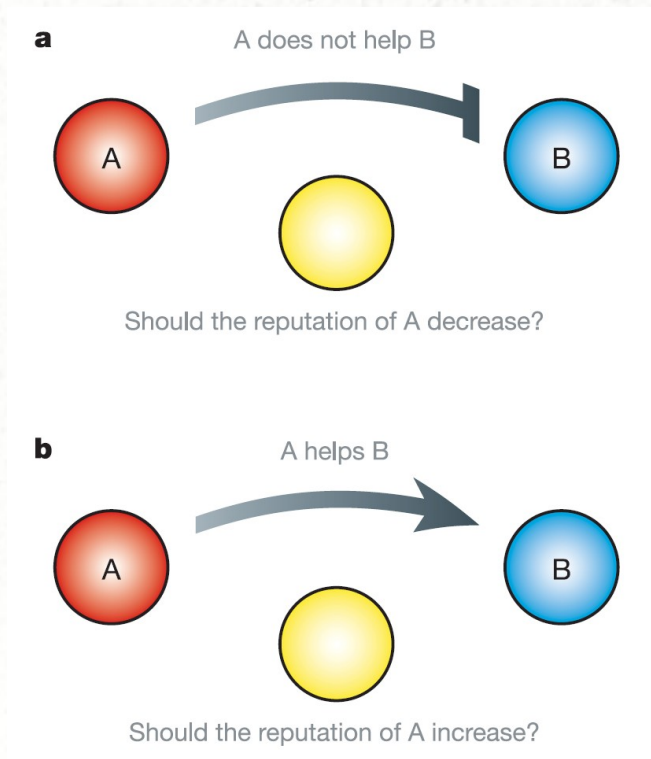
	C	D
C	$b - c$	$-c(1 - q)$
D	$b(1 - q)$	0

$$b - c > b(1 - q) \Rightarrow$$

$$q b > c$$

Aparición de códigos morales

Brandt & Sigmund (2004) J. Theor. Biol. **231**, 475-486



$$A = \{ \mathbf{C}, \mathbf{D} \} \quad \text{acciones}$$

$$R = \{ \mathbf{B}, \mathbf{M} \} \quad \text{reputaciones}$$

$$S = \{ R^2 \rightarrow A \} \quad \text{estrategias}$$

$$M = \{ A \times R^2 \rightarrow R \} \quad \text{códigos morales}$$

$$|S| = 2^4 = 16 \quad |M| = 2^8 = 256$$

$$|S \times M| = 2^{12} = 4096$$

Aparición de códigos morales

código moral

reputación del que da y del que recibe

		BB	BM	MB	MM
acción del que da	C	B	B	B	B
	D	M	M	M	M
	C	B	B	B	B
	D	M	B	M	M
	C	B	M	B	M
	D	M	B	M	M
	C	B	M	B	M
	D	M	M	M	M

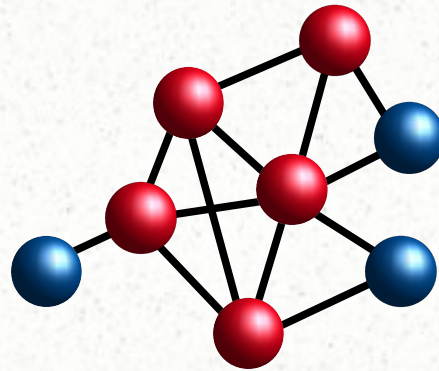
Aparición de códigos morales

las 8 imbatibles

	BB	BM	MB	MM	
C	B	*	B	*	juicio moral
D	M	B	M	*	
	C	D	C	*	acción

Estructura de la población

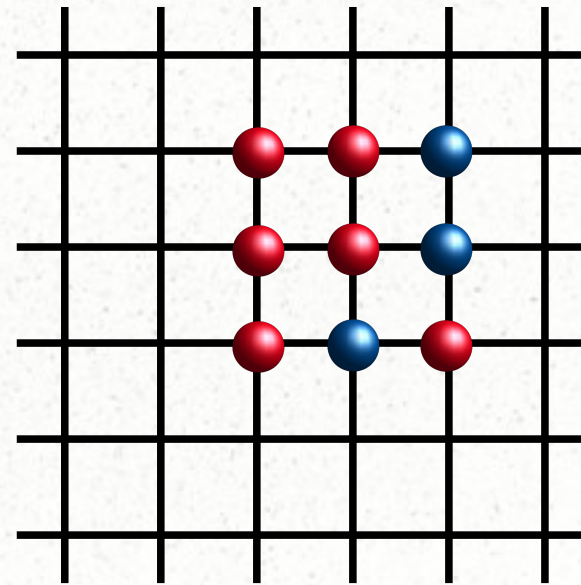
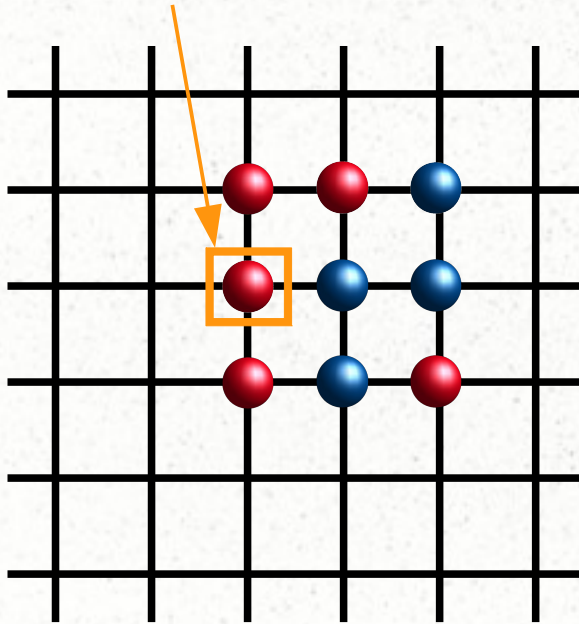
Nowak & May (1992) Nature **359**, 826-829



- Segregación por interactuar solo con los vecinos de una red de contactos
- La estructura puede ser espacial o una red social
- Funciona si la dinámica agrupa los cooperadores

Estructura de la población

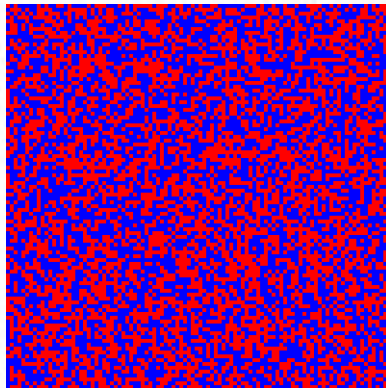
máxima ganancia



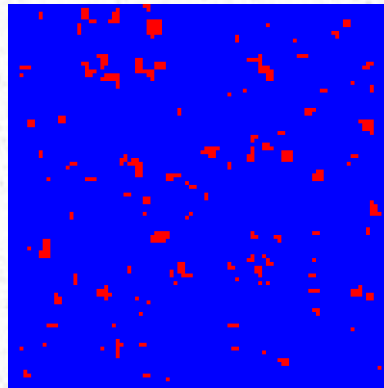
imitación incondicional

Estructura de la población

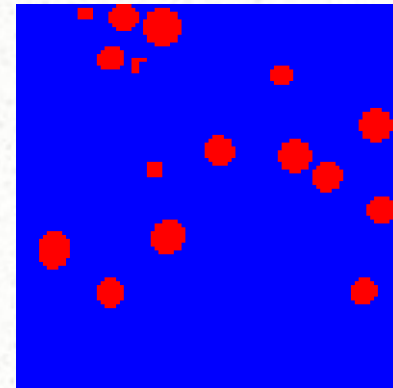
$$b = 1.2 \quad c = 0.2$$



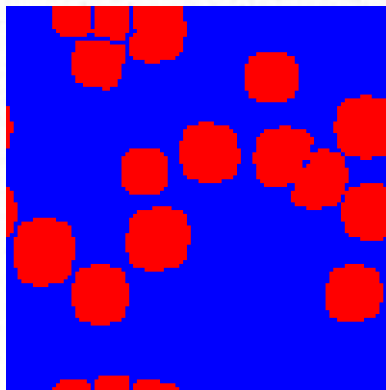
$t = 0$



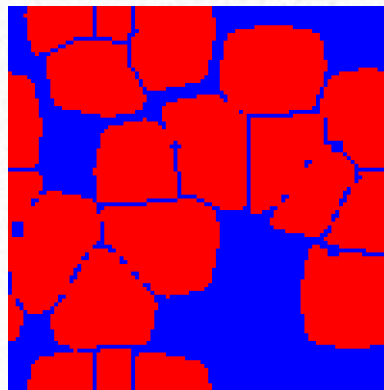
$t = 1$



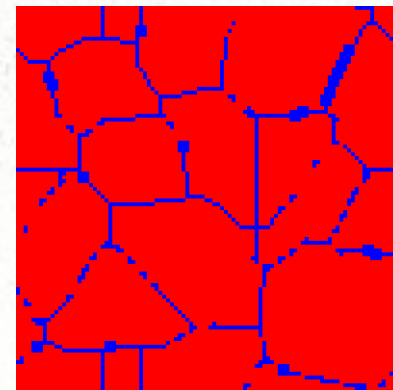
$t = 4$



$t = 9$



$t = 18$



$t = 35$

Competición entre plantas



ahorradoras



derrochadoras

$$F = k \phi$$

fitness eficiencia flujo de agua

$$\phi_a = \alpha \phi_d \quad (\alpha < 1)$$

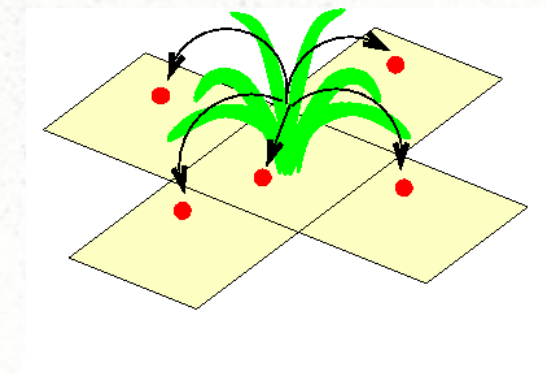
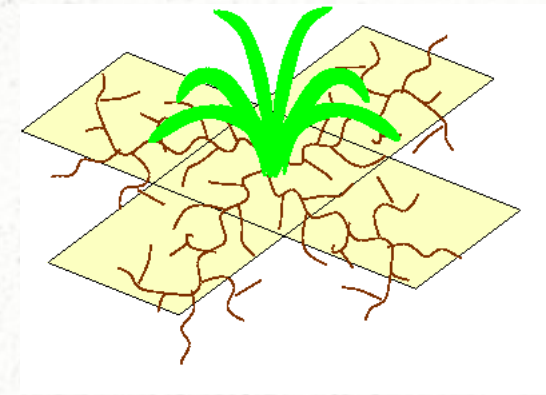
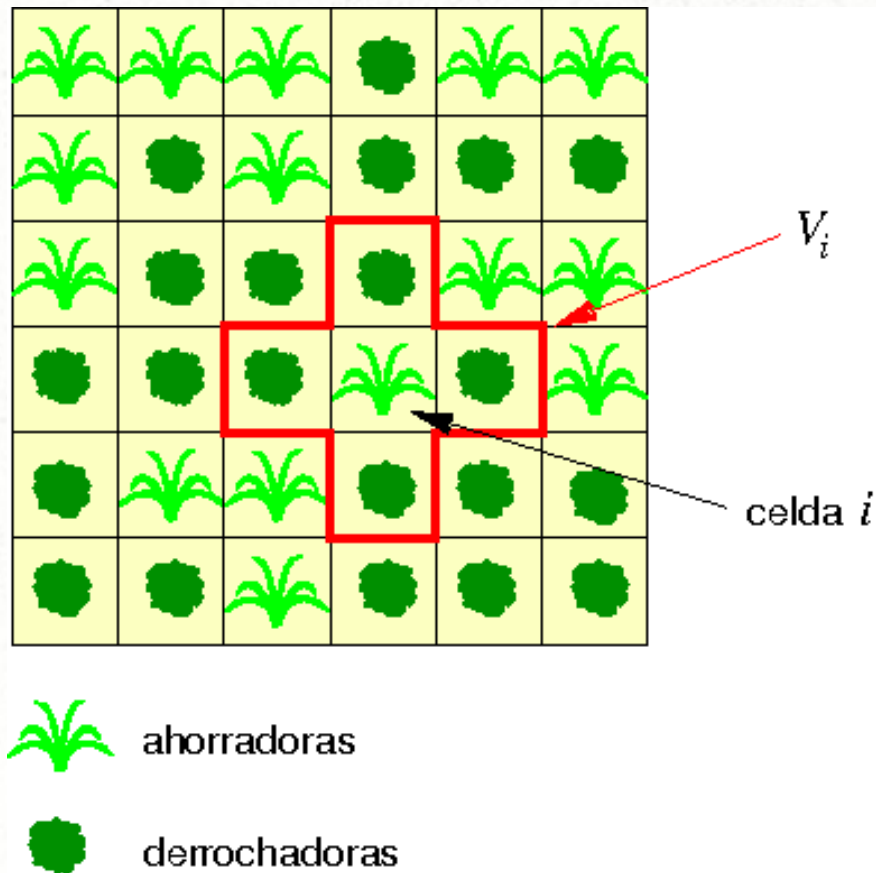
$$k_d = \kappa k_a \quad (\kappa < 1)$$

$$f_a = \frac{\alpha}{\alpha x + 1 - x}$$

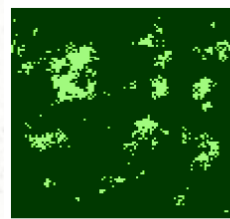
$$f_d = \frac{\kappa}{\alpha x + 1 - x}$$

$0 < \alpha < \kappa < 1 \rightarrow$ tragedia de los comunes

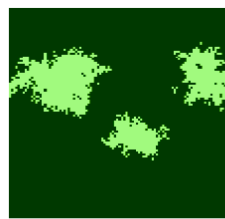
Competición entre plantas



Competición entre plantas



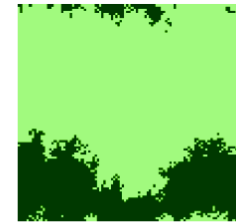
$t = 40$



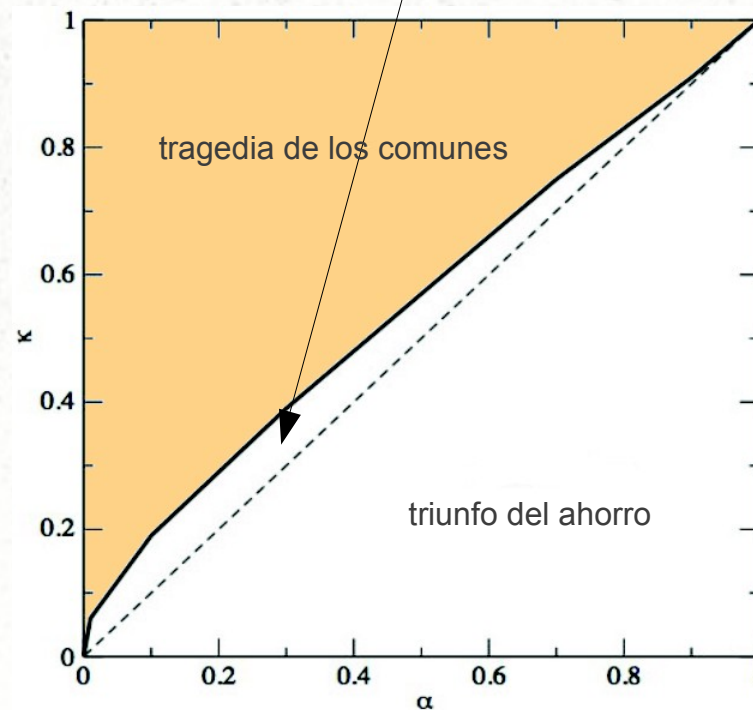
$t = 217$



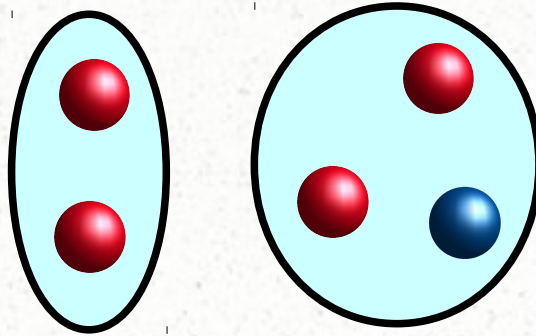
$t = 440$



$t = 630$



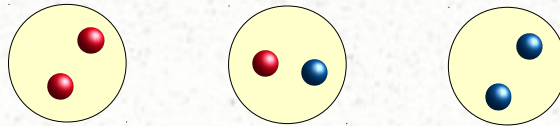
Selección de grupos



- Primer paso hacia una jerarquía de selección a diferentes niveles
- Los individuos son quienes se reproducen
- La selección actúa sobre los grupos

Selección de grupos

grupos de dos individuos



		
	$b-c$	$-c$
	$b/2$	0

$$\frac{1}{2}b < c \longrightarrow \text{group with two blue dots}$$

$$\frac{1}{2}b > c \longrightarrow \text{group with one red and one blue dot}$$

Conclusiones

- La Teoría de Juegos formaliza las interacciones estratégicas
- La TJ clásica resuelve enfrentamientos entre individuos racionales
- La TJ evolutiva adapta la TJ a poblaciones de individuos con distintos fenotipos
- La evolución por selección natural se presenta como un juego estratégico entre especies
- La Biología está llena de ejemplos susceptibles de ser descritos mediante juegos
- La aparición de comportamientos cooperativos es una de las áreas más activas de investigación en TJ evolutiva

A photograph of a man with a grey beard and mustache, wearing a blue shirt and a patterned tie, sleeping with his head tilted back in a lecture hall. Other people in the background are also sleeping or resting their heads on their desks. The text "Gracias por vuestra atención" is overlaid on the image.

**Gracias por
vuestra atención**